## **Solutions - Homework 1**

(Due date: January 17th @ 7:30 pm)

Presentation and clarity are very important! Show your procedure!

## PROBLEM 1 (50 PTS)

- Leading Zero Detector: This iterative circuit processes a 15-bit input (MSB first) and generates the number of leading 0's. before the first 1. Example:
  - $\checkmark~$  If the sequence is: 0000 0000 0011 010  $\rightarrow$  R = 10
  - $\checkmark~$  If the sequence is: 0001 0000 0011 010  $\rightarrow$  R = 3
  - ✓ If the sequence is: 0000 0000 1000 001  $\rightarrow$  R = 8
- The figure depicts the (in ASM form) and a datapath circuit. Note: Counters. If E=sclr=1, → Q=0. Input data: x (entered sequentially, MSB first). Output data R.
  - ✓ Complete the timing diagram of the digital circuit (next page). Note that 3 sequences are evaluated.
  - ✓ Write a structural VHDL code. You MUST create a file for i) modulo-(N+1) counter, ii) flip-flop, iii) Finite State Machine, and v) Top file (where you will interconnect all the components).
  - ✓ Write a testbench according to the timing diagram shown (next page). Simulate the circuit (Behavioral simulation). Verify that the simulation is correct by comparing it with the timing diagram you completed manually.
  - $\checkmark$  Upload the following files to <u>Moodle</u> (an assignment will be created):
    - VHDL code files
    - VHDL testbench

See attached .zip file: SolutionsHW1p1.zip



| clock     |                 |     |                | <u></u>  |                         |  |                    | <u>/</u>   |                             |                     |  | <u>ل</u>                                |  |   |  |                      |                  |      |             |
|-----------|-----------------|-----|----------------|--|-------------------------|--|--------------------|--|-----------------------------|---------------------|--|---|--|---|--|----------------------|------------------|------|-------------|
| resetn    |                 |     |                | 1  | <br> <br>               | :<br> <br>                                     | <br> <br>          | :<br> <br>   | <br> <br>                   |                     | <br> <br>  | <br> <br>                               | 1  |   | •<br> <br>                                 | <br> <br>            | <br> <br>        |      |             |
| start     |                 |     |                | <br> <br>  Y   | <br>                    | <br>   | <br>               | <br>   | <br>  <br>  ~~~             | ~                   | <br> <br> <br>   | <br> <br>  ~~.                          | <br> <br> <br>                                 | <br>  | <br>  <br>  7                              | <br>  <br>  %        | <br> <br> <br>   |      | I           |
| x         |                 |     | $1 \times 14$  | $\begin{pmatrix} \chi_{13} \\ 0 \end{pmatrix}$   | $1 \times 12$           | $1 \times 11$                                  | $\chi_{10}$        | $1 \times 10^{1}$  | $\frac{1}{1}$ $\frac{1}{1}$ | $\chi_{0}$          | $\frac{1}{1}\sqrt{\frac{1}{0}}$                              | $1 \times 1$                            | $\begin{pmatrix} \chi_4 \\ 0 \end{pmatrix}$    | $1 \times 10^{-1}$  | $\frac{1}{1}$ $\frac{1}{1}$                | $\frac{1}{\sqrt{0}}$ | $1 \\ 1 \\ 1$    | X 0  |             |
| R         | 0               | 0   |                | <u> </u>   | 2                       | <u> </u><br>  3                                | <u> </u>           | <u> </u> 5   | 6                           | 6                   | 6  | 6                                       | 6  | 6   |  | 6                    | 6                | 6    | 0           |
| Q         | 0               | 0   |                | +<br>1   | 2                       |  |                    |  |                             | 7                   |  | 1<br>1<br>1<br>9                        | 10   | 11  | 12   | 13                   | 14               | 15   |             |
| b         |                 |     | <br> <br>      | <br> <br>  | <br> <br>               | <br> <br>                                      | <br> <br>          | <br> <br>  | <br> <br>                   |                     | <br> <br>  | <br> <br>                               | <br> <br>                                      | <br> <br>   | <br> <br>                                  | <br> <br>            | <br> <br>        |      |             |
| Z         |                 |     | <br> <br>      | <br> <br>  | <br> <br>               | <br> <br>                                      | <br> <br>          | <br> <br>  |                             |                     | <br> <br>!   | <br> <br>!                              | <br> <br>                                      | <br> <br>   | <br> <br>!                                 | <br> <br>            | <br> <br>        |      |             |
| state     | s1              | S1  | L<br>  S2      | L<br>  | s2                      | L<br> <br> S2                                  | L<br> <br>  S2     | L<br> <br>  S2   | L<br> <br>  S2              | s2                  | s2   | s2                                      | s2   | S2  | <br> <br>  \$2                             | s2                   | s2               | s3   | S1          |
| done      |                 |     | <br> <br>      | <br> <br>  | <br> <br>               | <br> <br>                                      | <br> <br>          | <br> <br>  | <br> <br>                   | <br> <br>           | <br> <br>  | <br> <br>                               | <br> <br>                                      | <br> <br>   | <br> <br>                                  | <br> <br>            | <br> <br>        |      |             |
|           |                 |     | - · - · -      |  | ·                       |  |                    | I<br>- · - · -   |                             | I<br>- · - · - ·    |  |   |  |   |  |                      | I<br>- · - · - · |      |             |
| clock     | 1               |     |                | ケ∟   | ケ∟′                     |  |                    | <u>/</u>   |                             |                     |  |   |  |   |  |                      |                  |      |             |
| resetn    |                 |     | <br> <br>      | :<br> <br>   | <br> <br>               | :<br> <br>                                     | <br> <br>          | :<br> <br>   | <br> <br>                   |                     | <br> <br>  | <br> <br>                               | <br> <br>                                      | <br> <br>   | ;<br> <br>                                 | <br> <br>            | <br> <br>        |      | <br>        |
| start     |                 |     |                | <br>   | <br>                    | <br>!  | <br>               | <br>!  | <br>                        | <br>                | <br>   | <br>                                    | <br>   | <br>  | <br>!                                      | <br>                 | <br>             |      |             |
| х         | +               |     | $x_{14}$       | $\begin{array}{c} x_{13} \\ \hline x_{13} \\ \hline x_{10} \\ \hline x_{13} \\ x_{13} \\ \hline x_{13} \\ x_{13$ | $\frac{x_{12}}{x_{12}}$ | $\frac{x_{11}}{x_{11}}$                        | $\frac{x_{10}}{1}$ | $\begin{array}{c} & x_8 \\ \hline & x_8 \\ \hline & 0 \end{array}$ | $\frac{x_8}{1}$             | $x_7$               | $\frac{x_6}{x_6}$  | $\frac{x_5}{1}$                         | $\begin{array}{c} x_4 \\ x_4 \\ 0 \end{array}$ | $\begin{array}{c} x_3 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ $ | $\begin{bmatrix} x_2 \\ x_2 \end{bmatrix}$ | $x_{1}$              | $x_0$            | X 0  |             |
| R         | -               | 0   |                |  | <u> </u><br>  2         | 1<br>  3                                       | 4                  |  | 6                           | 7                   | <br> 8   | <br>  9                                 | 10   | <br> 11   | ' <u>11</u>                                | 1<br>11              | 11               | 11   | 0           |
| Q         |                 | 0   |                |  |                         |  |                    |  |                             | 7                   |  | <br>                                    | 10   | 11  | 12   | <br> <br> 13         | 14               | 15   | 0           |
| b         | +               |     | <br> <br>      | <br> <br>  | <br> <br>               | <br> <br>                                      | <br> <br>          | <br> <br>  | <br> <br>                   |                     | <br> <br>  | <br> <br>                               | <br> <br>                                      | <br> <br>   |  | <br> <br>            | <br> <br>        |      |             |
| Z         | _               |     | <br>           |  | <br>                    | <br>   | <br>               | <br>   |                             |                     | <br>   | <br>                                    | 1  |   |  |                      |                  |      |             |
| state     | _ L<br> <br>_ L | S1  | L              | L<br> <br>S2   | L<br>S2                 | L<br> <br>S2                                   | L<br> <br>  S2     | L<br> S2   | L<br> S2                    | S2                  | s2   | J<br> <br> S2                           | <br>   | S2  | <br> <br> S2                               | s2                   | s2               | s3   | S1          |
| done      |                 |     | <br> <br>      | <br> <br>  | <br> <br>               | <br> <br>                                      | <br> <br>          | <br> <br>  | <br> <br>                   | <br> <br>           | <br> <br>  | <br> <br>                               | <br> <br>                                      | <br> <br>   | <br> <br>                                  | <br> <br>            | <br> <br>        |      |             |
| - · - · · | '               | · · | I<br>- · - · - |  |                         |  |                    |  |                             | <br>                |  | <b>.</b> . <b>.</b> .                   | _ · _ · _                                      |   | <br>                                       |                      | <br>- · - · - ·  |      | · - · - · . |
| clock     | 1               |     |                | ケᢇ   |                         |  |                    |  |                             |                     |  |   |  |   | <u></u>                                    |                      |                  |      |             |
| resetn    |                 |     |                | 1  | 1                       | <br>   | 1                  | 1  | <br>                        | 1                   | 1  | 1                                       | 1  | 1   | <br>                                       | <br>                 | 1                |      |             |
| start     | -               |     | ¦L<br>¦r       | <br> <br>  Y   | <br> <br>  ~~           | <br>   | <br>  <br>  ~~~    | <br> <br>  7   | <br>  <br>  ~~~             | r                   | ι<br>Ι<br>Ι<br>Υ   | <br> <br>  Y.                           | γ<br>γ   | <br>  | <br>  <br>  Y                              | <br>  <br>  ~~~      | <br>             |      |             |
| х         | +               |     | $1 \times 14$  | $\begin{pmatrix} x_{13} \\ 0 \end{pmatrix}$  | $1 \times 12$           | $\begin{pmatrix} \chi_{11} \\ 0 \end{pmatrix}$ | $1 \times 10$      | $\begin{pmatrix} \chi_8 \\ 1 \\ 1 \\ 0 \\ \end{pmatrix}$           | $1 \times 10^{1}$           | $\chi^{-\lambda_7}$ | $\left  \begin{array}{c} x_6 \\ 1 \\ 1 \end{array} \right  $ | $\frac{1}{1}\sqrt{\frac{\lambda_5}{0}}$ | $1 \times 4$                                   | $1 \qquad x_3 \\ 1 \qquad 0$  | $1 \times 2$                               | $\chi^{\lambda_1}$   | $X_0$            | X 0  |             |
| R         | -+              | 0   |                | + ·<br>1 _ 1   | 1<br>1<br>2             | 1<br>  3                                       | 4                  | <u> </u>   | 6                           |                     | <br> 8   | <br> 9                                  | 10   | <br> 11   | 12   | 13                   | 14               | 15   | 0           |
| Q         |                 | 0   |                |  |                         |  |                    |  |                             | 7                   |  | 1<br>1<br>1 9                           | 10   | 11  |  | 13                   | 14               | 15   |             |
| b         | +               |     | <br> <br>      | <br> <br>  | <br> <br>               | <br> <br>                                      | <br> <br>          | <br> <br>  | <br> <br>                   |                     | <br> <br>  | <br> <br>                               |  | <br> <br>   | <br> <br>                                  | <br> <br>            | <br> <br>        |      |             |
| z         |                 |     | <br>           |  | <br> <br>               | <br> <br>                                      | <br> <br>          | <br> <br>  |                             |                     | <br> <br>  | <br> <br>                               | 1  |   | <br> <br>                                  |                      | <br>             |      | <br> <br>   |
| state     |                 | S1  | L<br> <br>S2   | L<br> S2   | L<br> <br>  S2          | L<br> <br>  S2                                 | 1<br> <br>  S2     | L<br> <br>  S2   | L<br>  S2                   | s2                  | s2   | s2                                      | s2   | s2  | I<br>IS2                                   | s2                   | s2               | <br> | s1          |
| done      |                 |     | <br> <br>      | <br> <br>  | <br> <br>               | <br> <br>                                      | <br> <br>          | <br> <br>  | <br> <br>                   | <br>                | <br> <br>  | <br> <br>                               |  | <br> <br>   | <br> <br>                                  | <br> <br>            | <br> <br>        |      |             |

2

Ρ

done

ready

PERIOD

COUNTER

ς

## PROBLEM 2 (30 PTS)

- **Period Counter**: It measures the period of a periodic input waveform with a precision of 1 ms (from 1 ms to 1000 ms).
  - ✓ Inputs: x (input waveform), s (start signal).



- ✓ Clock frequency: 100 Mhz.
- Operation: The circuit takes a measurement when the s signal (usually a clock pulse) is asserted. This amounts to count the number of cycles between two rising edges of the input waveform.
- However, to directly count the number of milliseconds, we can use a counter Q that counts up to 1 ms. Every time Q reaches 1 ms, we increase the count on another counter P, which will keep the number of milliseconds elapsed.
- The counter Q starts counting after the first rising edge is detected. When the second rising edge is detected, we assert done for a clock cycle. We are then ready to measure again should the signal s is asserted. The figure below shows an example for an input waveform whose period is 3 ms.



✓ Sketch the circuit: FSM + Datapath components. Specify all the I/Os of the FSM, as well as the signals connecting the FSM and the Datapath components.

Suggestion: The Datapath only needs two counters (Q and R) and a rising edge detector.

- Rising edge detector: It issues a one-cycle (10 ns) pulse on redg when it detects a rising edge on x.
- Counter Q: 1 ms counter. For a clock period of 10 ns, it counts from 0 to 10<sup>5</sup>-1.
- Counter P: It stores the period of x in ms. This counter counts from 0 to 999.

You can use the standard counter with *enable* and *sclr* inputs. If using a rising edge detector block, sketch its design (e.g.: State Machine)

✓ Provide the State Diagram (in ASM form) of the FSM.





## PROBLEM 3 (20 PTS)

Calculate the result of the following operations, where the operands are signed integers. For the division, calculate both the quotient and the residue. No procedure = zero points.

| 11001 1011 10101 10110 0111 | 10101 × | 01001 × | 101001 ÷ | 0111101 ÷ | 10011 ÷ |
|-----------------------------|---------|---------|----------|-----------|---------|
|                             | 11001   | 1011    | 10101    | 10110     | 0111    |



| ✓ | $\frac{101001}{10101} = \frac{-23}{-11}$ | 010111   |
|---|--|--|
|   | 00010                                    | To unsigned: $\frac{0.0111}{01011}$  |
|   | 1011 10111<br>1011↓                      | Unsigned Integer Division: $Q' = 10, R' = 1$<br>$\rightarrow Q = Q' = 010, \rightarrow R = -R' = 2C(01) = 1$ |
|   | 01                                       | Verification: $-23 = (-11 \times 2) - 1$   |

$$\checkmark \quad \frac{0111101}{10110} = \frac{61}{-10}$$

$$000110$$

$$1010 \qquad 1010 \qquad 1010 \qquad 1010 \qquad 1010 \qquad 1010 \qquad 01$$

$$Unsigned Integer Division: Q' = 110, R' = 1$$

$$\rightarrow Q = -Q' = 2C(0110) = 1010, \rightarrow R = R' = 01$$

$$\forall \quad \frac{10011}{0111} = \frac{-13}{7}$$
To unsigned:  $\frac{01101}{0111}$